Text S1. An illustration of how it is determined whether a host is successfully vaccinated or not. This demonstrates the use of the notation F to describe the set of host and virus types that are successfully vaccinated.

Consider a vaccine that contains 5 epitopes (n=5) restricted by 5 different HLA types:

Epitope number	1	2	3	4	5
HLA class I restriction	A1	A13	B51	B27	В7

An individual with HLA type A1, A2, B27, B8 would be host type  $\mathbf{h_a} = (1,0,0,1,0)$ . An individual with HLA type A1, A13, B51, B27 would be host type  $\mathbf{h_b} = (1,1,1,1,0)$ .

A virus with no escape mutations in any of the 5 epitopes would be virus type  $\mathbf{v}_a = (0,0,0,0,0)$ .

A virus with escape in the A1 and B27 epitopes would be virus type  $\mathbf{v}_b = (1,0,0,1,0)$ .

The set F contains  $(\mathbf{h_a}, \mathbf{v_a}), (\mathbf{h_b}, \mathbf{v_a})$  and  $(\mathbf{h_b}, \mathbf{v_b})$  but not  $(\mathbf{h_a}, \mathbf{v_b})$ .

Host type Virus type	$\mathbf{h_a} = (1, 0, 0, 1, 0)$ $\mathbf{v_a} = (0, 0, 0, 0, 0)$	$\mathbf{h_a} = (1, 0, 0, 1, 0)$ $\mathbf{v_b} = (1, 0, 0, 1, 0)$	$\mathbf{h_b} = (1, 1, 1, 1, 0)$ $\mathbf{v_a} = (0, 0, 0, 0, 0)$	$\mathbf{h_b} = (1, 1, 1, 1, 0)$ $\mathbf{v_b} = (1, 0, 0, 1, 0)$
Ticks and crosses representing the epitopes that do and don't provide protection	$(\sqrt{,}\times,\times,\sqrt{,}\times)$	(x,x,x,x,x)	$(,,,,\times)$	$(\times, \sqrt{,} \sqrt{,} \times, \times)$
In F? Hosts are protected if they have protection from at least one epitope.	Yes	No	Yes	Yes

Notice that we assume no difference in the survivorship or infectiousness of an  $\mathbf{h}_b$  host whether infected with a  $\mathbf{v}_a$  virus or a  $\mathbf{v}_b$  virus. Provided one non-escaped epitope is restricted, the host is successfully vaccinated.